

## The continuing story of two-photon exchange: results from the OLYMPUS experiment

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Over the past two decades, a discrepancy has emerged between two different techniques for measuring the proton's electromagnetic form factors. Unpolarized electron-proton cross section measurements paint a picture of the proton's internal structure that is incompatible with measurements from polarization transfer experiments. The leading hypothesis is that the discrepancy is caused by a typically neglected radiative correction, hard two-photon exchange (TPE), which would affect the two measurement techniques in different ways. There is no model independent way to calculate hard TPE, but it can be measured experimentally by looking for an asymmetry between the positron-proton and electron-proton elastic cross sections. Three recent experiments have attempted to quantify this asymmetry, and, just last month, the third of these, called OLYMPUS, released its results [1]. The OLYMPUS experiment collected data in 2012 at DESY, alternating between 2 GeV electron and positron beams, directed through a hydrogen gas target. The scattered lepton and recoiling proton were detected in coincidence with a large acceptance toroidal spectrometer. The relative luminosity between the two beam species was monitored with three independent systems, and the results comprise 3 inverse fb of integrated luminosity, exceeding by a factor of three the other two TPE experiments combined. In this talk, the case for the TPE hypothesis will be presented, the OLYMPUS experiment will be described, and the results of all three experiments will be compared.

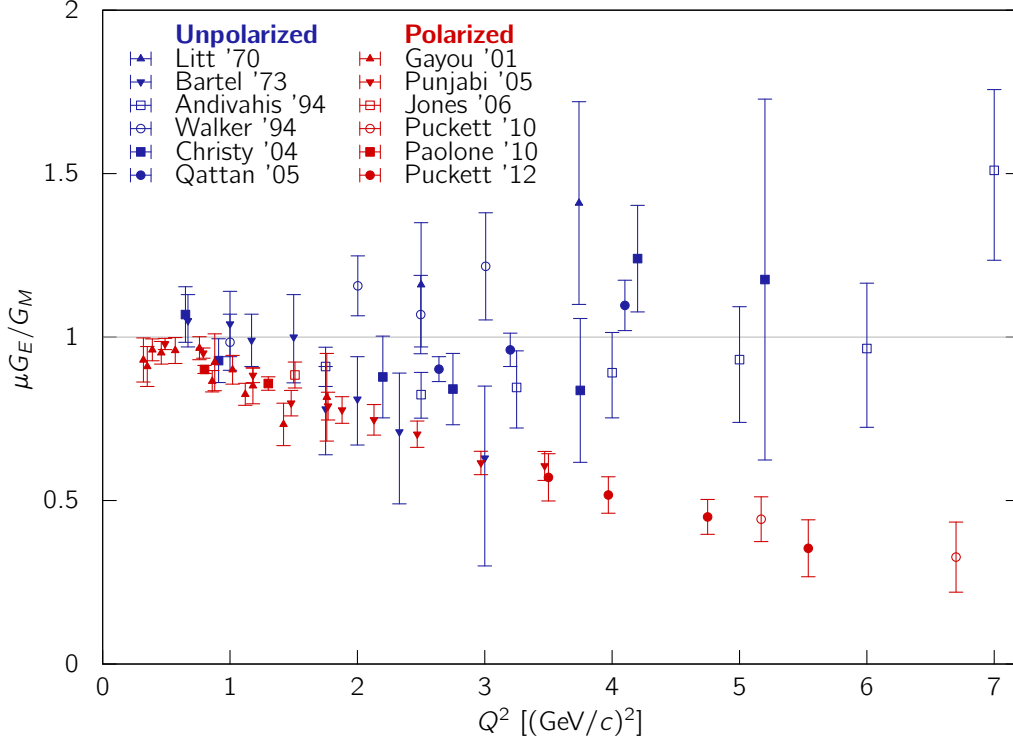
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## 1. Introduction



**Figure 1:** Measurements of the proton's form factor ratio  $\mu_p G_E/G_M$  extracted from polarization asymmetries [2–7] do not agree with those from unpolarized Rosenbluth separation [8–13].

Over the past few decades, a discrepancy emerged between two different techniques for measuring the proton's elastic electromagnetic form factors. These form factors,  $G_E(Q^2)$  and  $G_M(Q^2)$ , describe the proton's distributions of charge and current respectively as functions of the momentum transfer scale  $Q^2$ . Since the 1950s, the proton's form factors were extracted from unpolarized electron-scattering cross sections using Rosenbluth Separation [14]. The advent of high-quality polarized electron beams made it possible to extract the ratio  $G_E/G_M$  from double spin asymmetries. The two techniques have produced discrepant results, as can be seen in the representative sample of world data shown in figure 1. Until this discrepancy is understood, it is difficult to have complete confidence in our understanding of the proton's electromagnetic structure.

The leading hypothesis for the cause of the discrepancy is hard two-photon exchange hard TPE, which can be measured by taking the ratio of positron-proton to electron-proton elastic scattering cross sections. Three recent experiments have measured this ratio to test the TPE hypothesis, and with the recent release of the OLYMPUS results [1], all three have published their findings. The results are not strongly conclusive. OLYMPUS measured the ratio to be smaller than many predictions, but the results are still consistent with hard TPE being the cause of the discrepancy.

## 2. Why measure $\sigma_{e^+p}/\sigma_{e^-p}$ ?

The leading hypothesis for the cause of the proton form factor discrepancy is that there is

a non-negligible contribution from hard two-photon exchange (TPE), a radiative correction that is neglected in standard radiative correction prescriptions [15, 16]. If hard TPE were properly accounted for, it is possible that the polarization asymmetry and Rosenbluth separation measurements would actually be consistent with each other. Unfortunately, there is no model independent method for calculating hard TPE, though there are numerous model-dependent approaches, such as using hadronic intermediate states [17–19], dispersion relations [20–22], generalized parton distributions [23], and phenomenological fits [24–26]. Many predictions suggest that the inclusion of hard TPE would resolve the form factor discrepancy, while some disagree [27, 28].

Though there is no model independent calculation of hard TPE, it can be determined experimentally through a measurement of  $R_{2\gamma}$ , the cross section ratio of elastic positron-proton scattering to elastic electron-proton scattering (after standard radiative effects have been accounted for):

$$R_{2\gamma} \equiv \frac{\sigma_{e^+p \rightarrow e^+p}}{\sigma_{e^-p \rightarrow e^-p}} \quad (2.1)$$

At leading order, this ratio is equal to unity. The next to leading order term is an interference between one- and two-photon exchange. This interference term changes sign when switching between electron and positron scattering, so that  $R_{2\gamma}$  can be written:

$$R_{2\gamma} = 1 + \frac{4\text{Re}[\mathcal{M}_{2\gamma}^\dagger \mathcal{M}_{1\gamma}]}{|\mathcal{M}_{1\gamma}|^2} + \mathcal{O}(\alpha^4). \quad (2.2)$$

Deviations in  $R_{2\gamma}$  from unity indicate a contribution from hard TPE.

In addition to its magnitude, the kinematic dependence of  $R_{2\gamma}$  is also relevant. For TPE to help resolve the discrepancy,  $R_{2\gamma}$  should increase as  $\epsilon$ , the virtual photon polarization parameter, decreases and as momentum transfer  $Q^2$  increases.

### 3. Experiments

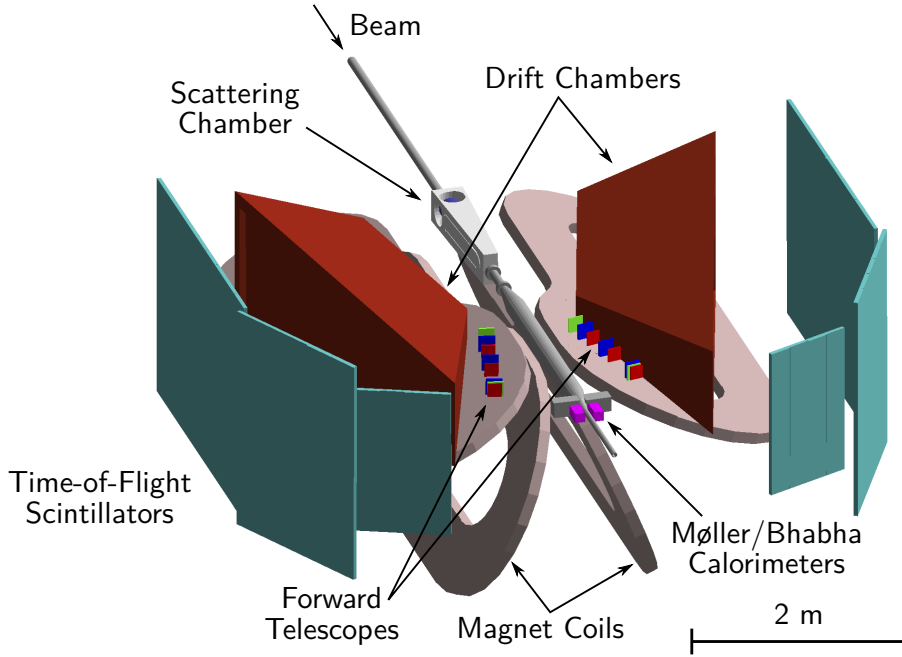
Three recent experiments endeavored to measure  $R_{2\gamma}$ . In addition to OLYMPUS, an experiment at the VEPP-3 storage ring in Novosibirsk, Russia, collected data in 2009 and 2012, and an experiment using the CLAS spectrometer in Hall B at Jefferson Lab, USA, collected data in 2011. Summaries of these experiments are presented below.

#### 3.1 The OLYMPUS Experiment

The OLYMPUS experiment [29] was conducted in 2012 at the DORIS storage ring at DESY, Hamburg, Germany. DORIS was modified so as to facilitate the acceleration and storage of electrons or positrons within the ring. During data collection, the beam species was alternated approximately once per day.

The DORIS beam was directed through a windowless hydrogen gas target that was internal to the ring vacuum [30]. A differential pumping system of six turbomolecular vacuum pumps was necessary to continuously remove the hydrogen gas that flowed from the ends of the target and prevent it from spoiling the ring vacuum.

The target was surrounded by a large-acceptance toroidal magnetic spectrometer. An illustration of the spectrometer is shown in figure 2. The spectrometer was previously used in the BLAST



**Figure 2:** The OLYMPUS spectrometer was formerly used in the BLAST experiment.

experiment [31], which ran from 2001–2005 at MIT-Bates. The spectrometer had two instrumented sectors, one to the left and the other to the right of the target chamber. Layers of drift chambers were used for tracking charged particles, and walls of scintillator were used for time-of-flight measurements and triggering. Elastic  $ep$  events were identified by a coincidence detection of the scattered lepton in one sector and the recoiling proton in the other.

In order to extract  $R_{2\gamma}$ , it was crucial to determine the relative luminosity between the electron and positron data sets. For this purpose, three independent luminosity monitoring systems were employed. By recording the instantaneous beam current as well as the target flow, the slow control system could reconstruct the relative luminosity to within a few percent. A pair of tracking telescopes were deployed at forward angles to monitor the rate of elastic  $ep$  scattering in kinematics where TPE effects were thought to be small. A pair of calorimeters were positioned next to the downstream beamline to measure the rate of symmetric Møller and Bhabha scattering [32].

### 3.2 Experiment at VEPP-3

The experiment at VEPP-3 was similar to OLYMPUS in that it used alternating stored beams of electrons and positrons [33]. However, elastic  $ep$  events were detected in a non-magnetic detector. This came with the advantage of having identical acceptances for detecting electrons and positrons. However, without a magnetic field, no momentum analysis of the detected particles was possible. The rejection of inelastic background relied on energy deposition measurements in CsI, NaI, and scintillator detectors.

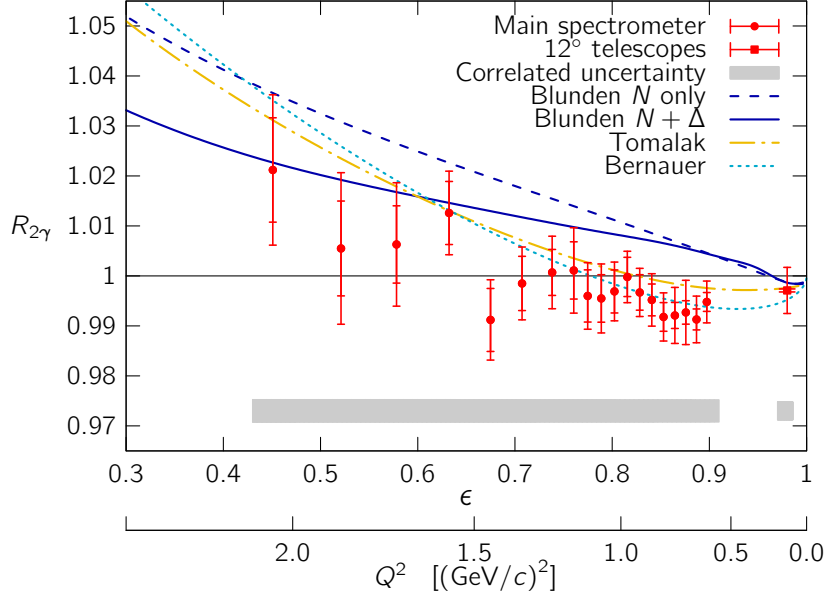
The relative luminosity between electron and positron modes was also a concern for the VEPP-3 experiment. The luminosity was normalized to the forward elastic scattering point, at kinematics

where TPE effects are expected to be small. Thus, the VEPP-3 measurement of  $R_{2\gamma}$  is relative to  $R_{2\gamma}$  at their luminosity normalization point (LNP).

### 3.3 CLAS Two-Photon Experiment

The CLAS Two-Photon Experiment [34–36] used a tertiary beam of electron/positron pairs. The Hall B secondary photon beam was directed on gold converter foil to create electron and positron pairs, which in turn were directed through a magnetic chicane so that the unconverted photons to be blocked. By combining measurements taken in both chicane polarities, the luminosity of electron and positron data sets could be guaranteed to be equal. However, given the tertiary beam, the initial pre-scatter energy of the lepton in each event was unknown and had to be reconstructed. Scattered leptons and recoiling protons were detected in the CLAS spectrometer, a toroidal magnetic spectrometer with nearly  $4\pi$  coverage.

## 4. Results

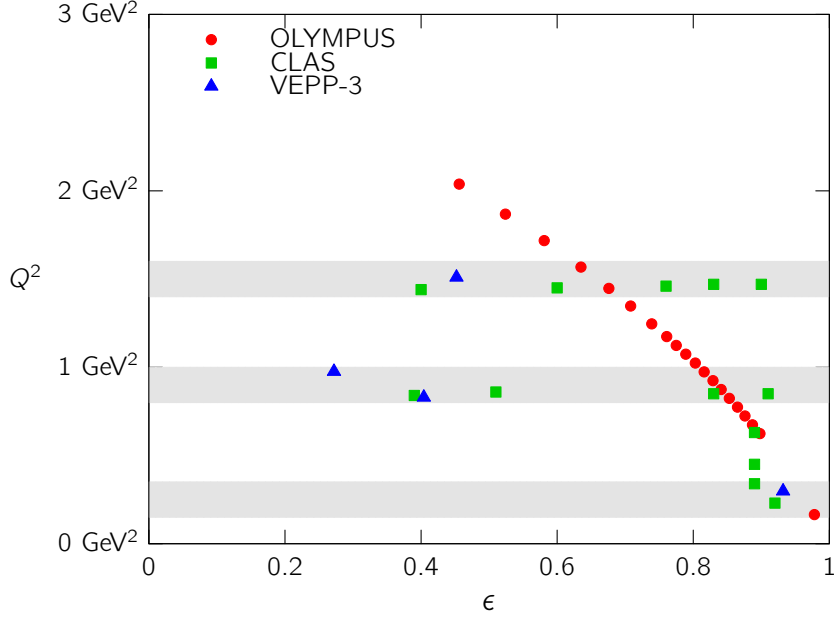


**Figure 3:** OLYMPUS measured  $R_{2\gamma}$  to be somewhat lower than theoretical calculations by Blunden et al. [22], and Tomalak et al. [21], and the phenomenological prediction by Bernauer et al. [26].

The results of the OLYMPUS experiment [1] are shown in figure 3, along with three predictions for  $R_{2\gamma}$ . The inner error bars show the statistical uncertainty, while the outer error bars show the statistical and uncorrelated systematic uncertainties added in quadrature. The grey band below the data shows the  $1\sigma$  correlated uncertainty, though the correlations are more complicated than a simple scale factor, and will be described in a future article. The predictions from Blunden et al. use a dispersive approach to calculate the TPE diagrams with hadronic propagators; the  $N$ -only prediction assumes only a nucleon propagator only, while  $N + \Delta$  assumes the coherent sum of nucleon and  $\Delta$  propagators [22]. The calculation of Tomalak et al. uses subtracted dispersion relations to evaluate the TPE diagrams [21]. The curve shown corresponds to a subtraction point of  $\epsilon = 0.5$ .

The phenomenological prediction of Bernauer et al. comes from fits to world form factor data with an assumed functional form for the TPE contribution [26].

OLYMPUS measures  $R_{2\gamma}$  to be somewhat smaller than predicted. The OLYMPUS data are for the most part consistent with unity over much the OLYMPUS acceptance, and in fact fall below unity at low  $Q^2$  and high  $\epsilon$ , which is a prediction of Bernauer (and to a lesser extent, Tomalak). The slope of the data points is better matched by the Blunden calculations.



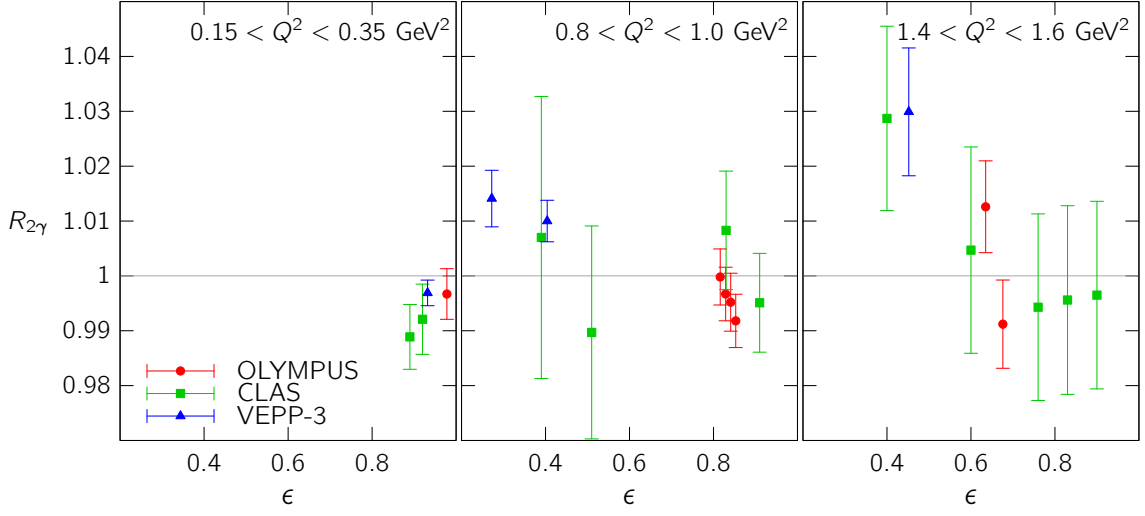
**Figure 4:** The results of the three recent TPE experiments are difficult to compare to one another because they are situated at different positions on the two-dimensional  $\epsilon, Q^2$  kinematic plane.

It is not straight-forward to compare the results of the three TPE experiments, because the kinematics of elastic scattering are two-dimensional. Figure 4 shows the kinematics for the data points of all three experiments in the  $\epsilon, Q^2$  plane. There is no reason that data points at similar values of  $\epsilon$  be consistent with each other, if they fall at very different values of  $Q^2$ . To permit a comparison, I show, in figure 5 the data in three bands of very similar  $Q^2$ , which are illustrated by gray bars in figure 4. In all three  $Q^2$  regions, there are no inconsistencies between the three experiments.

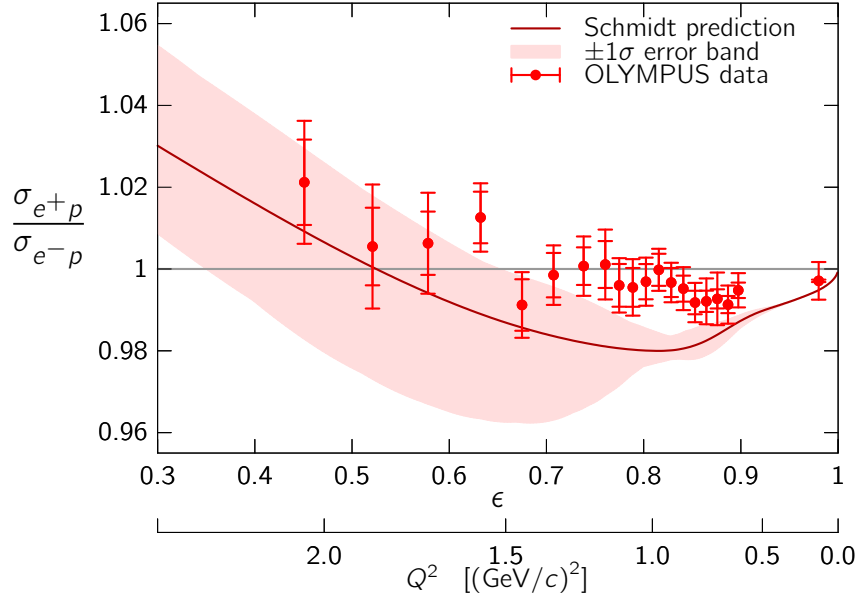
## 5. Conclusions

The results from OLYMPUS neither favor the null hypothesis (no hard TPE) because they show a slope in  $R_{2\gamma}$ , nor do they strongly confirm the TPE hypothesis. OLYMPUS measured  $R_{2\gamma}$  to be smaller than most theoretical predictions. This raises the possibility that there may be some unconsidered effects which must be added to the present theory calculations.

The important question that must be asked of the TPE results is whether or not the measured  $R_{2\gamma}$  resolves the form factor discrepancy. In an attempt to answer that question, I developed a phenomenological scheme for estimating the necessary  $R_{2\gamma}$  from global fits to polarized and unpolarized measurements of the proton's form factors (details are described in appendix D of [37]).



**Figure 5:** OLYMPUS measured  $R_{2\gamma}$  to be somewhat lower than theoretical calculations by Blunden et al. [22], and Tomalak et al. [21], and the phenomenological prediction by Bernauer et al. [26].



**Figure 6:** The amount of TPE needed to resolve the form factor discrepancy is not precisely determined, as seen by the uncertainty band from the phenomenological prediction of the author.

Global fits that are published with uncertainties allow an estimate of the uncertainty in the phenomenological prediction. Figure 6 shows the results for OLYMPUS kinematics. The input global fits for unpolarized data are taken from [26], while for the polarized data, the parameterization  $\mu_p G_E/G_M = 1 - 0.12Q^2/\text{GeV}^2$  was used. The uncertainty band is derived from the quoted uncertainties in [26]. As can be seen from the figure, the OLYMPUS measurement was made in kinematics in which little hard TPE is needed to resolve the discrepancy. Furthermore, the size of the needed TPE effect is not well constrained, especially for  $Q^2 > 1 \text{ GeV}^2$ . At these larger values of  $Q^2$ , the OLYMPUS data are fully consistent with the phenomenological prediction, which implies

that the TPE hypothesis is still completely valid.

For a more definitive test to rule out confirm the TPE hypothesis, a higher beam energy (and thus greater momentum transfer) is needed. At these kinematics, the form factor discrepancy is larger, and so the size of the needed TPE effect is greater, making it easier to distinguish between the hypotheses.

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